

# **Mathematics-1 Sets and Functions**

**Topics :** <u>Computer engineering</u> Written on <u>March 06, 2024</u>

"Sets and Functions" is a fundamental topic in mathematics that serves as the building block for many other mathematical concepts. Here's an overview of what this chapter typically covers:

#### 1. Introduction to Sets:

- Definition of a set: A collection of distinct objects.
- Representation of sets: Roster notation, set-builder notation.
- Cardinality of sets: Number of elements in a set.
- Subsets and supersets: Relationship between sets where every element of one set is also an element of another set (subset) or vice versa (superset).
- Universal set: Set containing all the objects under consideration.

#### 2. Types of Sets:

- $\circ\,$  Finite set: A set with a countable number of elements.
- $\circ\,$  Infinite set: A set with an uncountable number of elements.
- Empty set (null set): A set with no elements.
- Singleton set: A set with exactly one element.
- Equal sets: Sets having exactly the same elements.
- Power set: Set of all subsets of a given set.
- 3. Operations on Sets:
  - $\circ\,$  Union of sets: Combination of all elements from two or more sets.
  - Intersection of sets: Elements common to all sets.
  - Difference of sets: Elements present in one set but not in another.
  - Complement of a set: Elements not belonging to the set within a universal set.
  - $\circ\,$  Cartesian product: Set of all ordered pairs from two sets.

#### 4. Venn Diagrams:

- Graphical representation of sets using circles or rectangles.
- $\circ\,$  Illustration of set operations (union, intersection, difference, complement) using Venn diagrams.

## 5. Functions:

 $\circ~$  Definition of a function: A relation between two sets where each input has exactly one output.

- $\circ\,$  Domain and range: Set of all possible inputs and outputs of a function, respectively.
- $\circ\,$  Types of functions: One-to-one (injective), onto (surjective), and bijective functions.
- $\circ\,$  Composite functions: Combination of two or more functions.
- $\circ\,$  Inverse functions: Function that "undoes" the original function.

#### 6. Special Functions:

- $\circ\,$  Identity function: Function where the output is equal to the input.
- Constant function: Function where the output is the same constant value for all inputs.
- $\circ\,$  Polynomial function: Function defined by a polynomial expression.

Sure, let's illustrate "Sets and Functions" with examples:

Sets:

#### • Finite Set Example:

- Let's consider a set A = {1, 2, 3, 4}. This is a finite set because it has a countable number of elements.
- Another example of a finite set could be the set of weekdays: B = {Monday, Tuesday, Wednesday, Thursday, Friday}.

#### • Infinite Set Example:

- The set of natural numbers: N = {1, 2, 3, ...} is an infinite set because it continues indefinitely.
- Similarly, the set of real numbers is also infinite.

## • Empty Set Example:

- Let's denote the empty set as Ø or {}. It is a set with no elements.
- For example, the set of even numbers that are odd: C = {x | x is an even number and x is odd} = Ø.

## • Union and Intersection Example:

Let A = {1, 2, 3} and B = {3, 4, 5}. The union of A and B is A ∪ B = {1, 2, 3, 4, 5}.
The intersection of A and B is A ∩ B = {3}.

## • Complement Example:

• Let's consider a universal set  $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ . If  $A = \{2, 4, 6, 8\}$ , then the complement of A is  $A' = \{1, 3, 5, 7, 9, 10\}$ .

## • Functions:

## • One-to-One (Injective) Function Example:

- Let's define a function f: A  $\rightarrow$  B where A = {1, 2, 3} and B = {a, b, c} such that f(1) = a, f(2) = b, and f(3) = c.
- This function is one-to-one because each element in A maps to a unique element in

Β.

## • Onto (Surjective) Function Example:

- Consider a function g:  $A \rightarrow B$  where  $A = \{1, 2, 3\}$  and  $B = \{a, b\}$ . Let g(1) = a, g(2) = b, and g(3) = b.
- This function is onto because every element in B is mapped to by at least one element in A.

#### • Composite Function Example:

- Suppose we have two functions f:  $X \rightarrow Y$  and g:  $Y \rightarrow Z$ . Let  $f(x) = x^2$  and g(y) = 2y.
- The composite function  $h(x) = g(f(x)) = 2(x^2)$ .

## • Inverse Function Example:

- Let's define a function f: A → A where A =  $\{1, 2, 3, 4\}$  such that f(1) = 2, f(2) = 3, f(3) = 4, and f(4) = 1.
- The inverse function of f, denoted as f^(-1), would be such that f^(-1)(2) = 1, f^(-1)(3) = 2, f^(-1)(4) = 3, and f^(-1)(1) = 4.

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